



Einstein Equivalence Principle test with RadioAstron: preliminary results

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Introduction



RadioAstron:

- Proposal-driven space-VLBI observatory
- 10 m dish in space
- 1.35; 6; 18; 92 cm wavelengths
- tracking stations: Russia & US

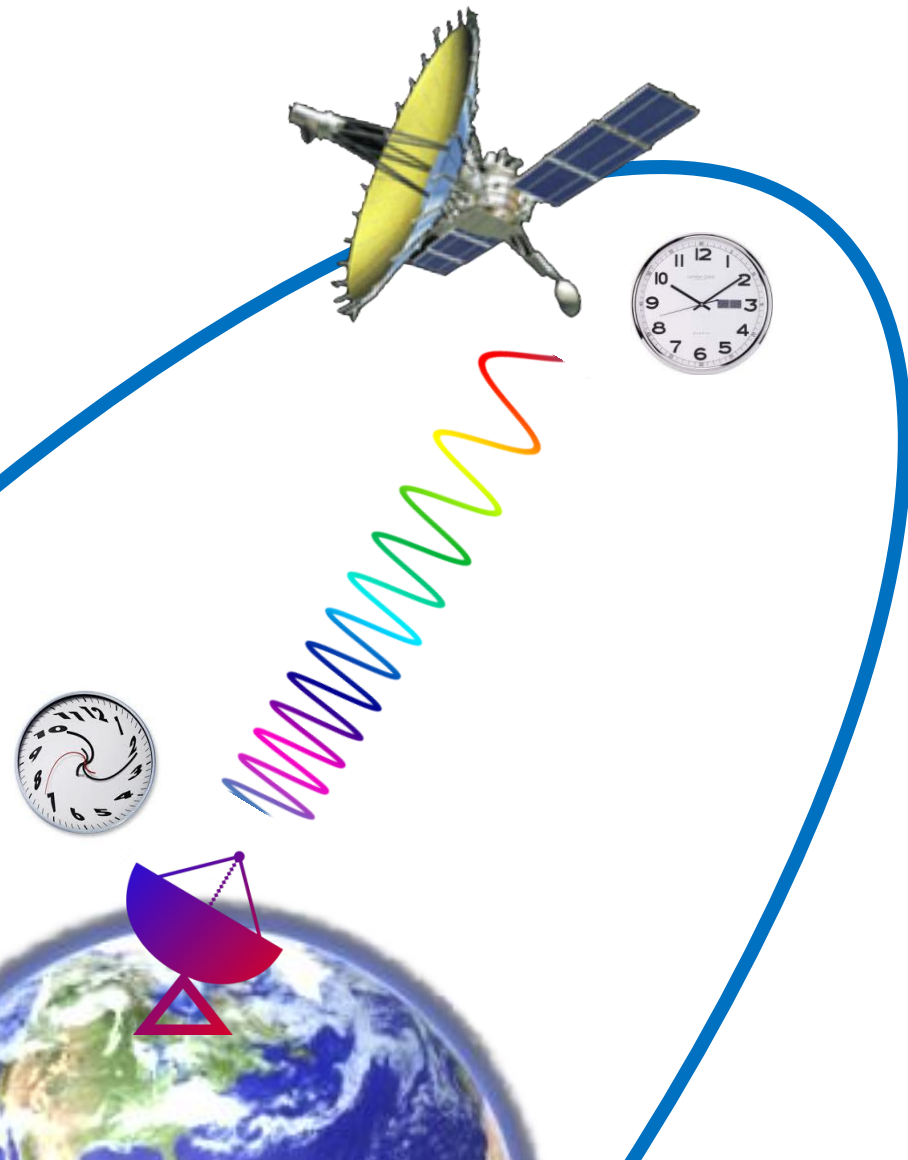
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Important for the gravitational redshift experiment:

- on-board hydrogen maser
- highly eccentric 9 day orbit

Experiment outline

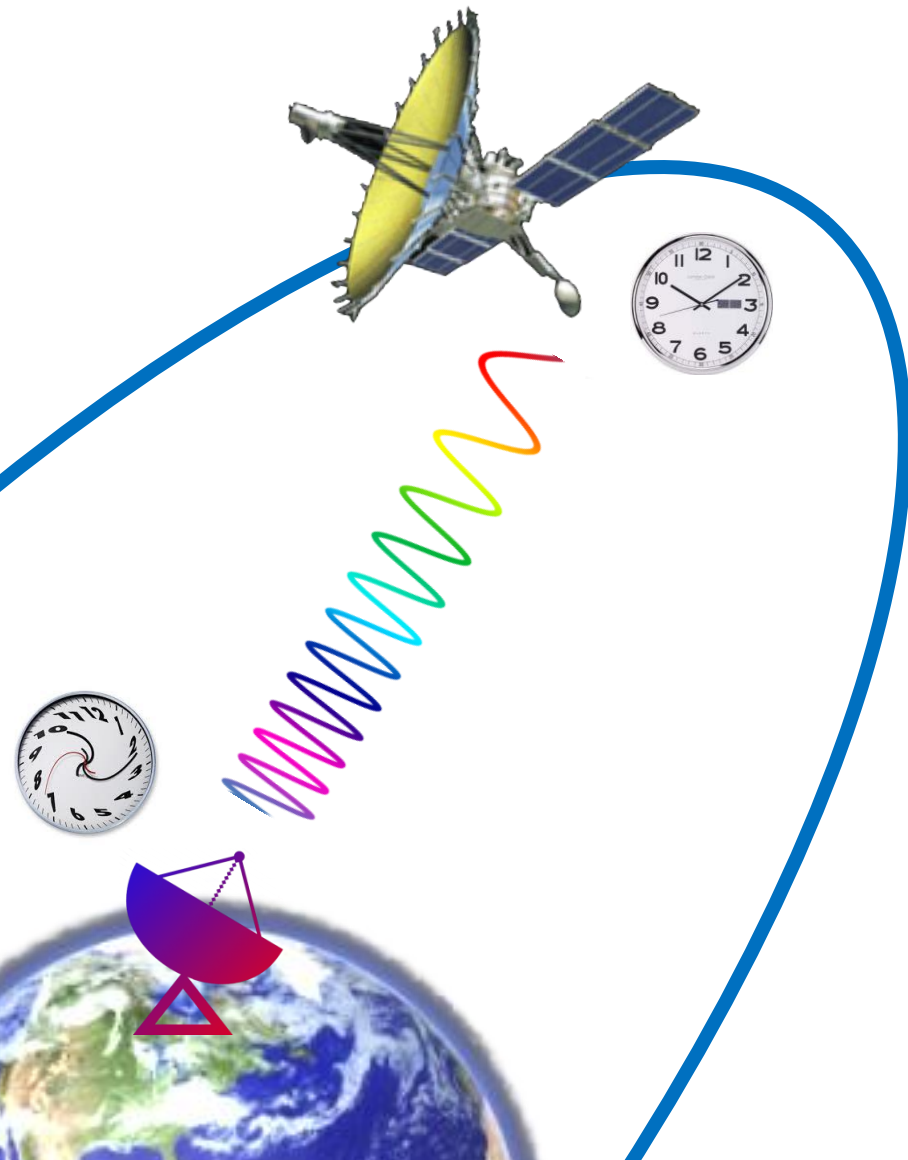


- frequency-based approach
- downlink at 8.4 and 15 GHz
- uplink at 7.2 GHz

Einstein Equivalence Principle:

$$\frac{\Delta f_{\text{grav}}}{f} = \frac{\Delta U}{c^2}$$

Experiment outline



- frequency-based approach
- downlink at 8.4 and 15 GHz
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Einstein Equivalence Principle:

$$\frac{\Delta f_{\text{grav}}}{f} = \frac{\Delta U}{c^2}$$

or

$$\frac{\Delta f_{\text{grav}}}{f} = \frac{\Delta U}{c^2} (1 + \varepsilon) \quad ?$$

Grand Unification:
$$\frac{\Delta f_{\text{grav}}}{f} = \frac{\Delta U}{c^2} (1 + \varepsilon)$$

violation parameter 

Possible mechanisms: Local Position Invariance broken
(dark matter halo, etc.)

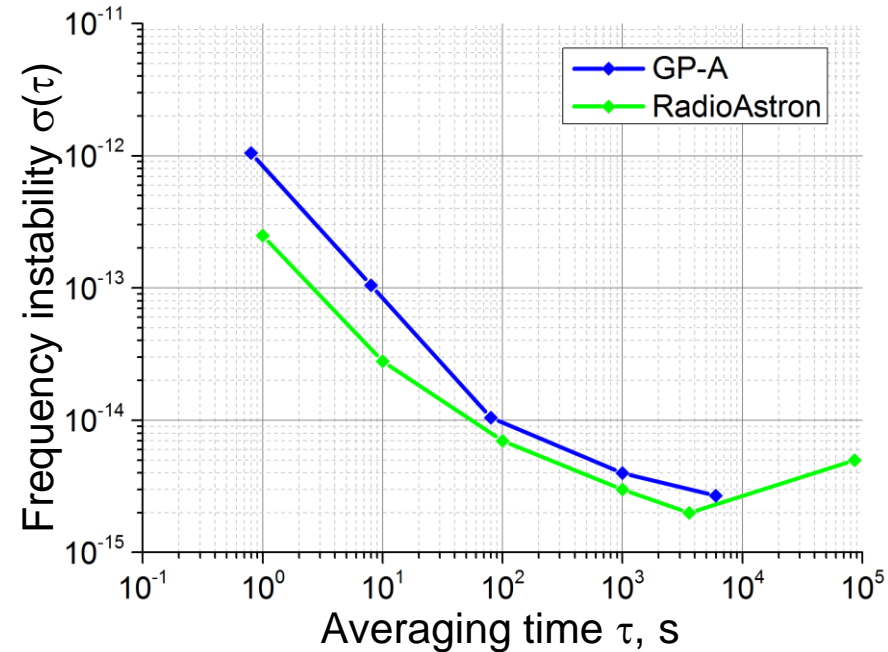
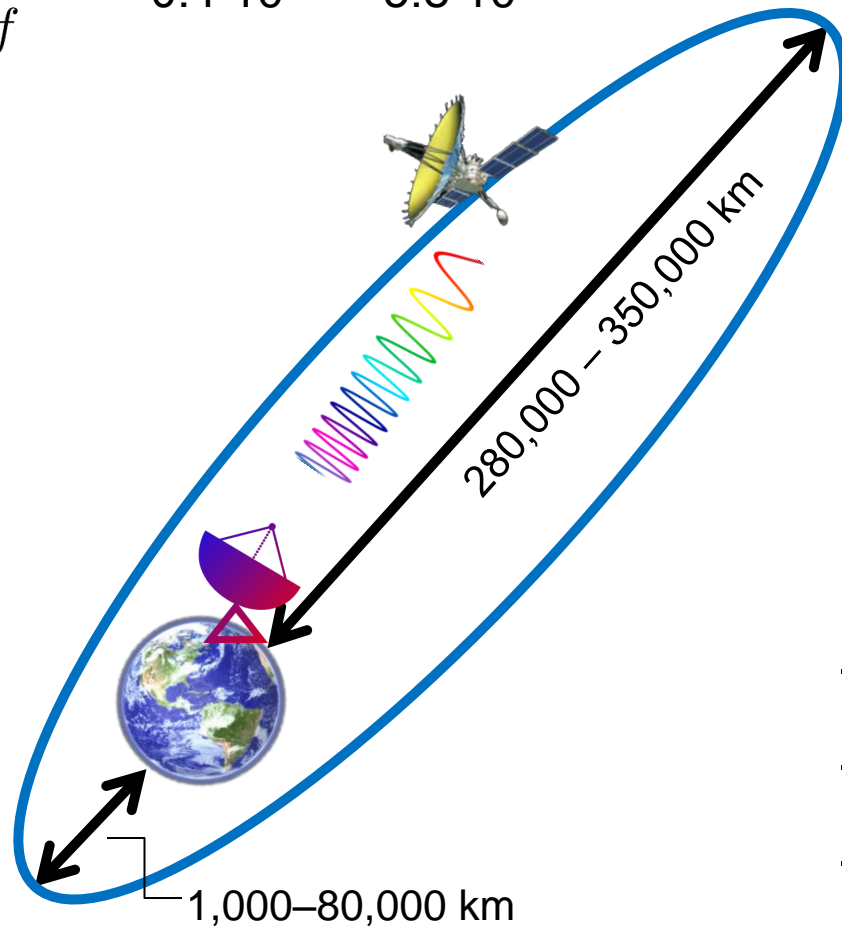
Violation magnitude: difficult to predict

Consequences: new physics, satellite navigation

RadioAstron gravitational redshift experiment prerequisites

Grav. redshift modulation:

$$\frac{\Delta f_{\text{grav}}}{f} = 0.4 \cdot 10^{-10} - 5.8 \cdot 10^{-10}$$



RadioAstron vs. Gravity Probe A:

- more stable H-maser
- greater modulation of the effect
- multiple measurements

Estimated accuracy: $\delta\varepsilon = (1-2) \times 10^{-5}$

Fractional frequency shift of the spacecraft downlink:

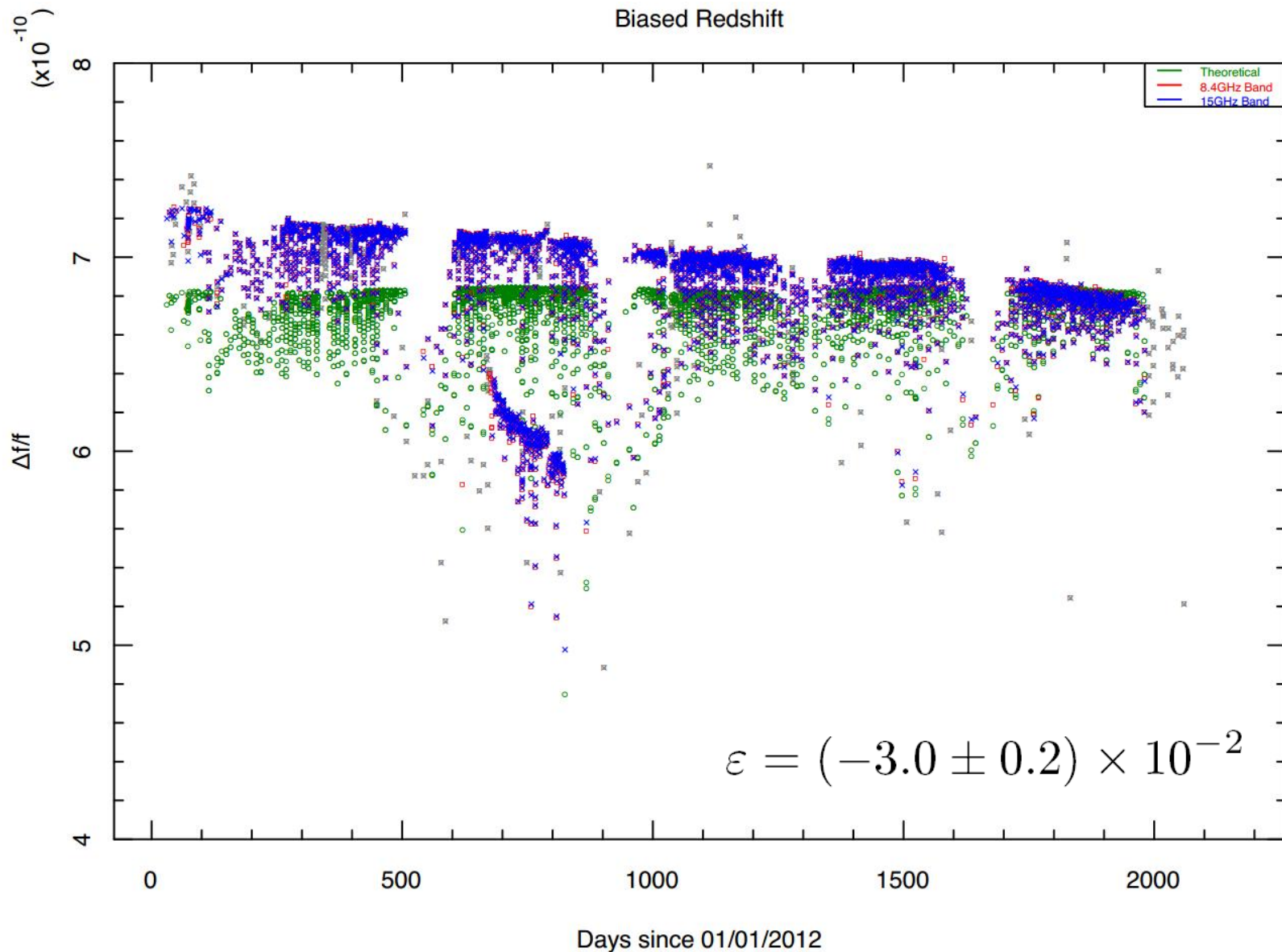
$$\begin{aligned} \frac{\Delta f}{f} = & -\frac{\dot{D}}{c} - \frac{v_s^2 - v_e^2}{2c^2} + \frac{(\vec{v}_s \cdot \vec{n})^2 - (\vec{v}_e \cdot \vec{n}) \cdot (\vec{v}_s \cdot \vec{n})}{c^2} \\ & + \frac{\Delta U}{c^2} + \frac{\Delta f_{\text{trop}}}{f} + \frac{\Delta f_{\text{ion}}}{f} + \frac{\Delta f_{\text{instr}}}{f} + O\left(\frac{v}{c}\right)^3 \end{aligned}$$

Pro: 6 years of radio science data

Con: orbit reconstruction accuracy

$$\dot{D} \sim 0.5 \text{ mm/s} \quad \rightarrow \quad \delta\varepsilon \sim 2 \times 10^{-3}$$

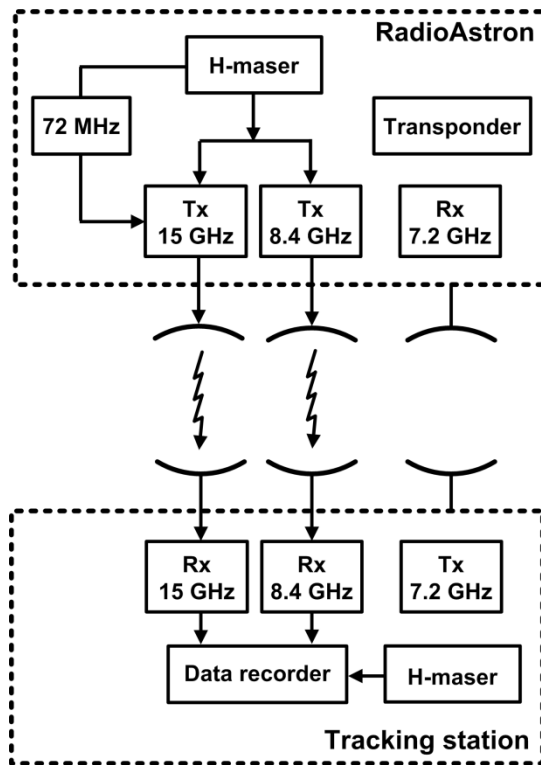
One-way data analysis results



Interleaved mode approach

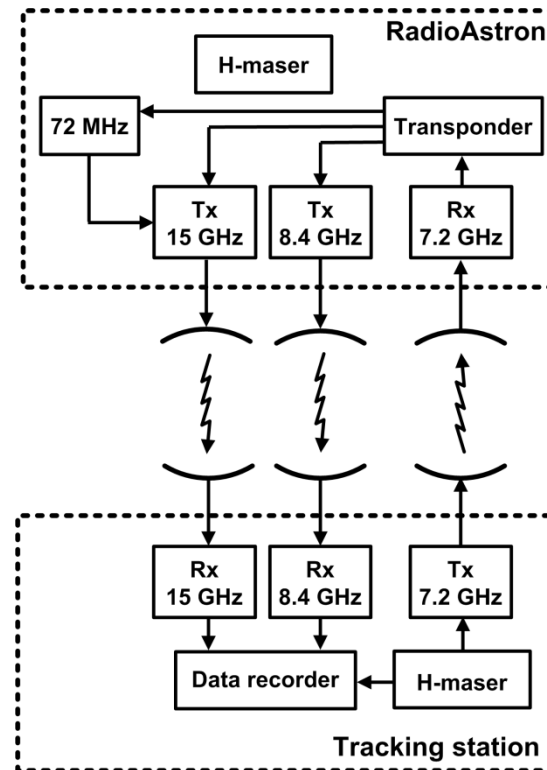
Solution: 1-way downlink – from the on-board H-maser
 2-way phase-locked loop – from the ground H-maser

**1-way
“H-maser”**



$$\frac{\Delta f_{1w}}{f} = -\frac{\dot{D}}{c} + \dots$$

**2-way
“Coherent”**



$$\frac{\Delta f_{2w}}{f} = -\frac{2\dot{D}}{c} + \dots$$

Biriukov+14

$$\Delta f_{1w} - \frac{1}{2} \Delta f_{2w} = \Delta f_{\text{grav}} + \Delta f_0 + f_0 \left(-\frac{|\mathbf{v}_s^2 - \mathbf{v}_e^2|}{2c^2} + \frac{\mathbf{a}_e \cdot \mathbf{n}}{c} \Delta t \right) + \Delta f_{\text{ion}}^{(\text{res})} + \Delta f_{\text{fine}} + O(v/c)^4$$

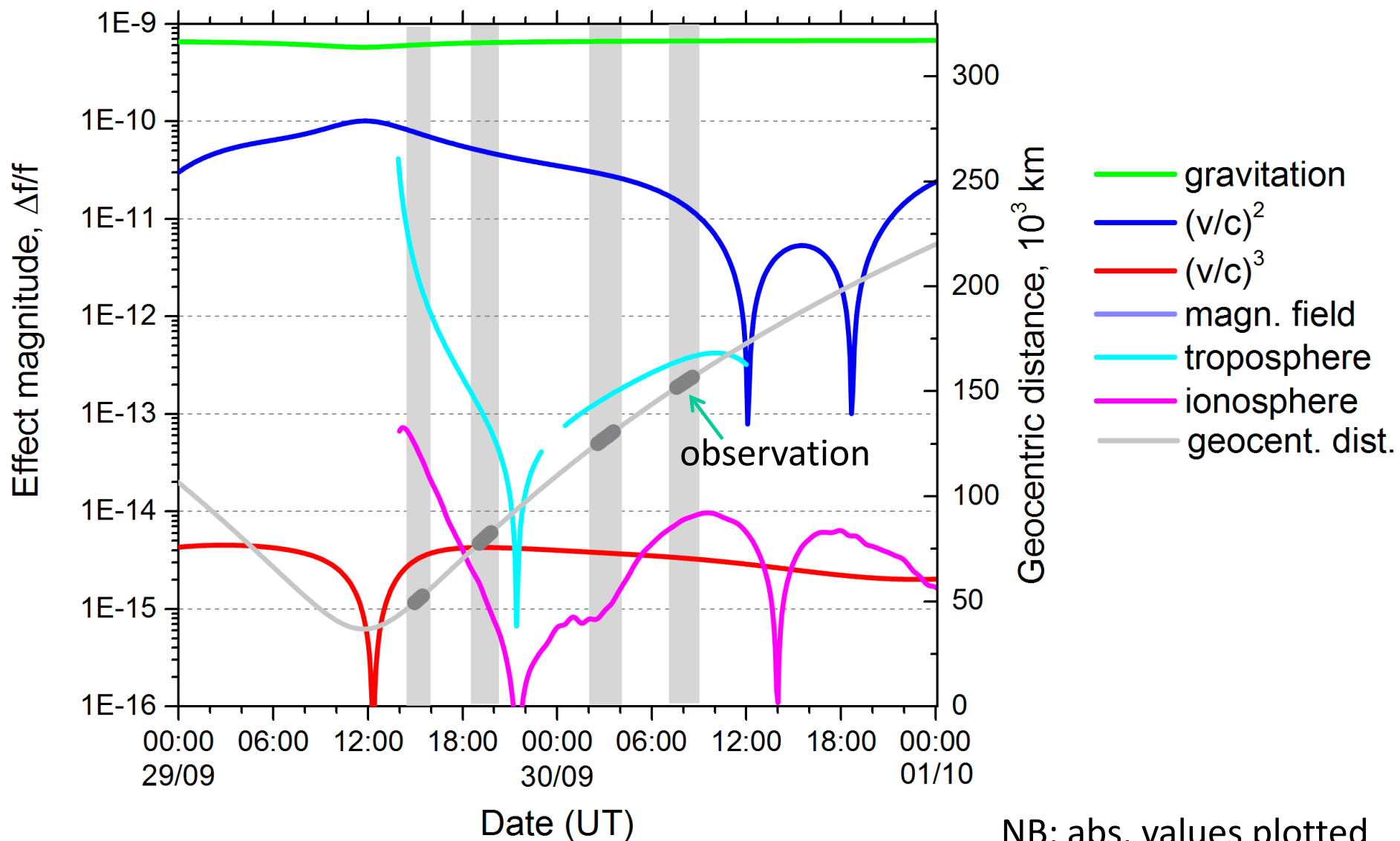
NB: nonrelativistic Doppler and tropospheric shifts are compensated, ionospheric shift is reduced by a factor of 6

Fine effects: $(v/c)^3$ kinematics, phase center motion, temperature and magnetic sensitivity of the H-masers

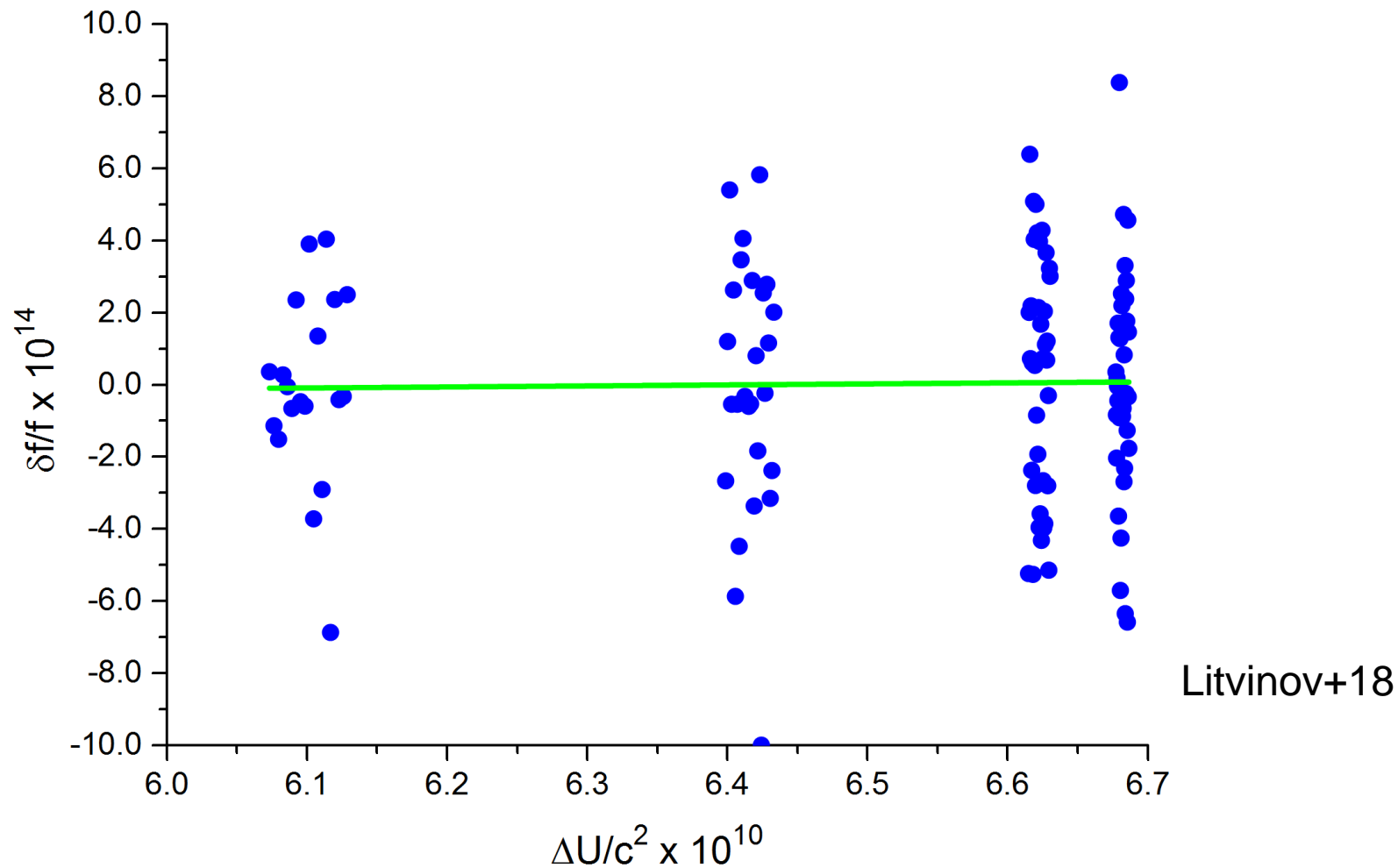
Final step – regression analysis:

$$\frac{\Delta f_{\text{grav}}}{f} = \frac{\Delta U}{c^2} (1 + \varepsilon)$$

Data: Gb, Ef, Hh, On, Sv, VLBA, Wn, Wz, Yg, Ys, Zc + tracking stations



NB: abs. values plotted



$$\frac{\delta f}{f} = \frac{\Delta f_{\text{grav}}}{f} - \frac{\Delta U}{c^2} = \varepsilon \frac{\Delta U}{c^2}$$

Gravity Probe A: $\varepsilon = (0.05 \pm 1.4) \times 10^{-4}$

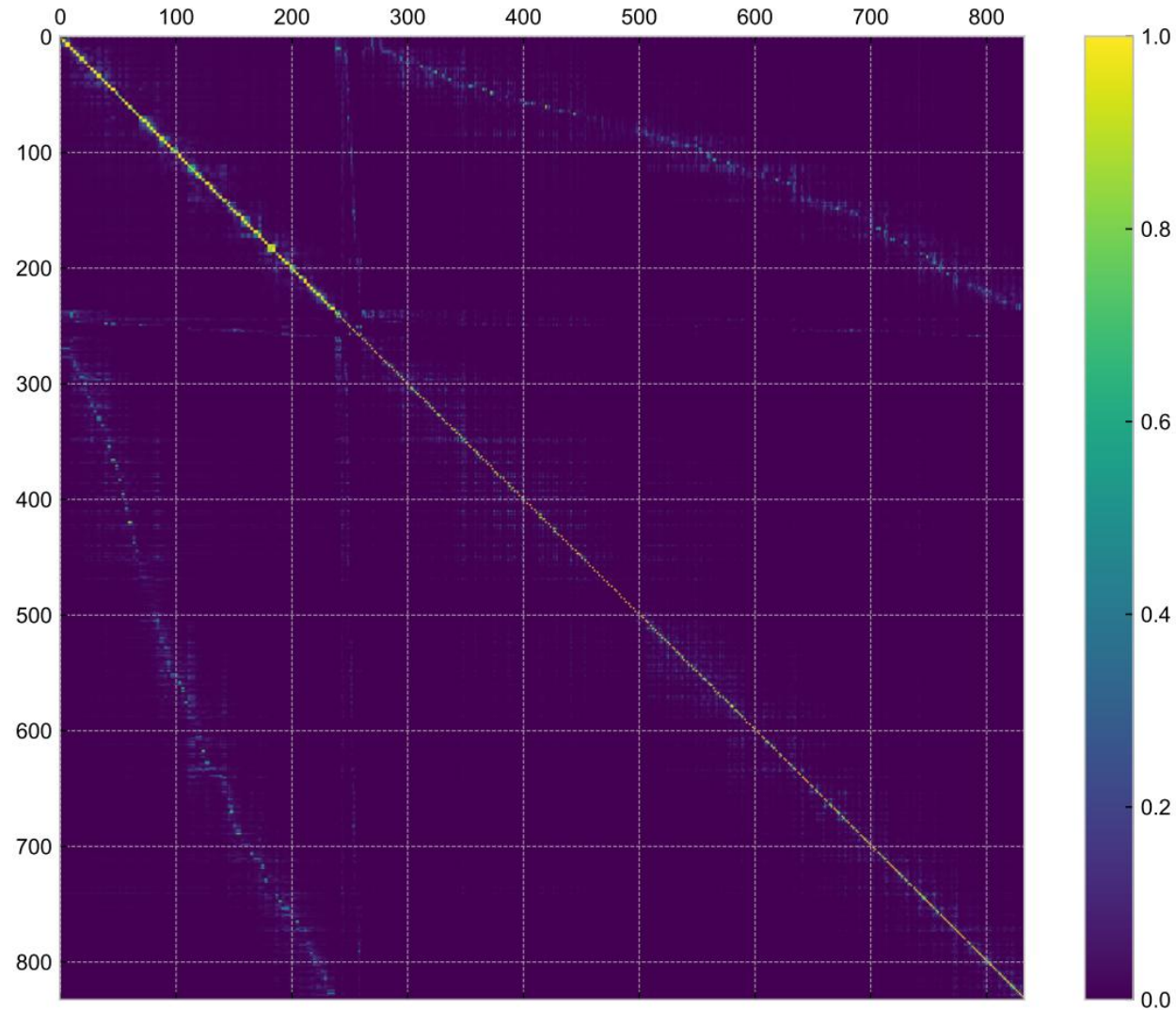
RadioAstron: $\varepsilon = (0.3 \pm 1.7) \times 10^{-4}$

How large are systematic errors?
How much does ε depend on tracking station position,
our knowledge of solar radiation pressure, etc.?

Over 800 parameters solved for, including the EEP violation parameter

(Others: spacecraft state vector, SRP coefficients, reaction wheel unloading, etc.)

Covariance matrix based on analysis of March 2017 data

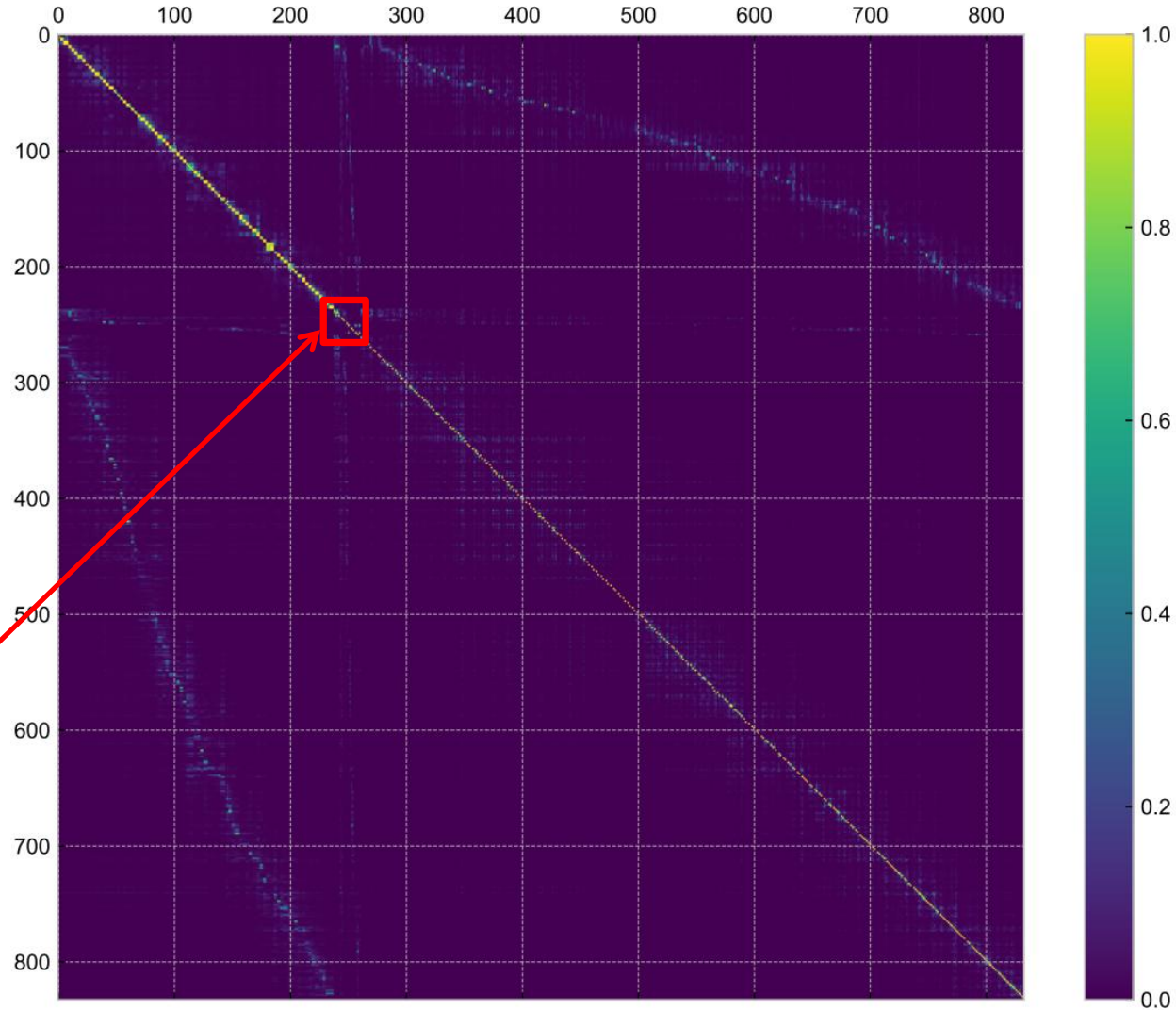


Covariance matrix based on analysis of March 2017 data

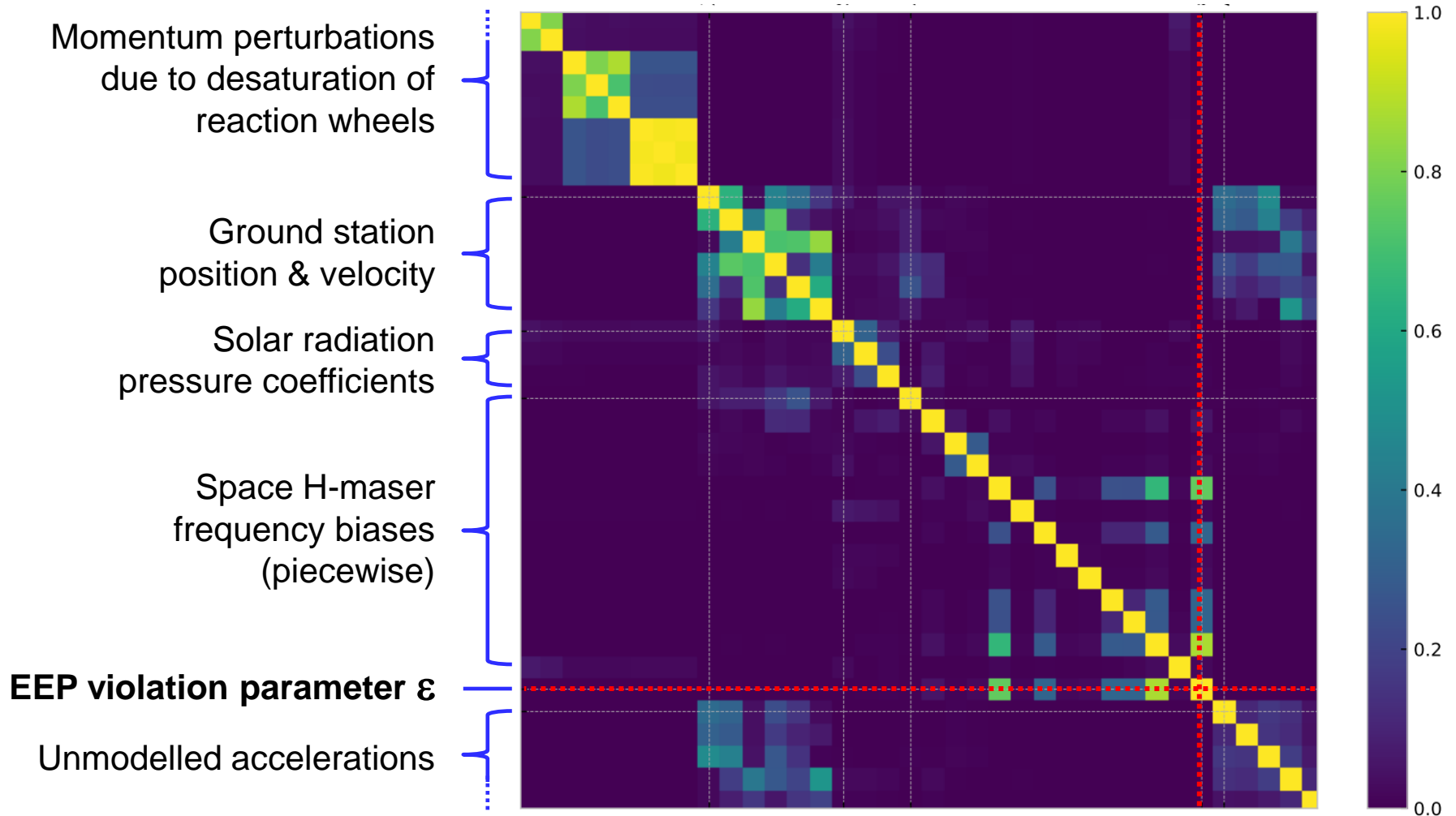
Over 800 parameters solved for, including the EEP violation parameter

(Others: spacecraft state vector, SRP coefficients, reaction wheel unloading, etc.)

Let's zoom into this area



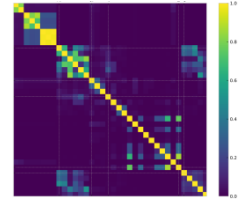
Systematic errors: covariance analysis



ϵ is correlated only with the space H-maser frequency biases

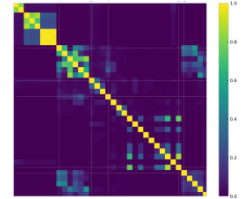
Lessons from the covariance analysis:

1. EEP violation parameter ε is correlated only with the space H-maser frequency biases.



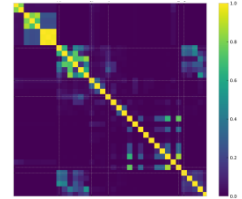
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1. EEP violation parameter ε is correlated only with the space H-maser frequency biases.
2. Independent measurement of these biases is required – done in calibration observations.
3. Other parameters are harmless, e.g. tracking station position uncertainty up to 1 meter is ok.



Well-known fact:

Redshift violation parameter ε may depend on clock type and element composition of the gravitational field source, e.g. its ratio of neutrons to protons. Possible clock dependence is exploited in null-redshift tests.

New (Wolf & Blanchet, 2016):

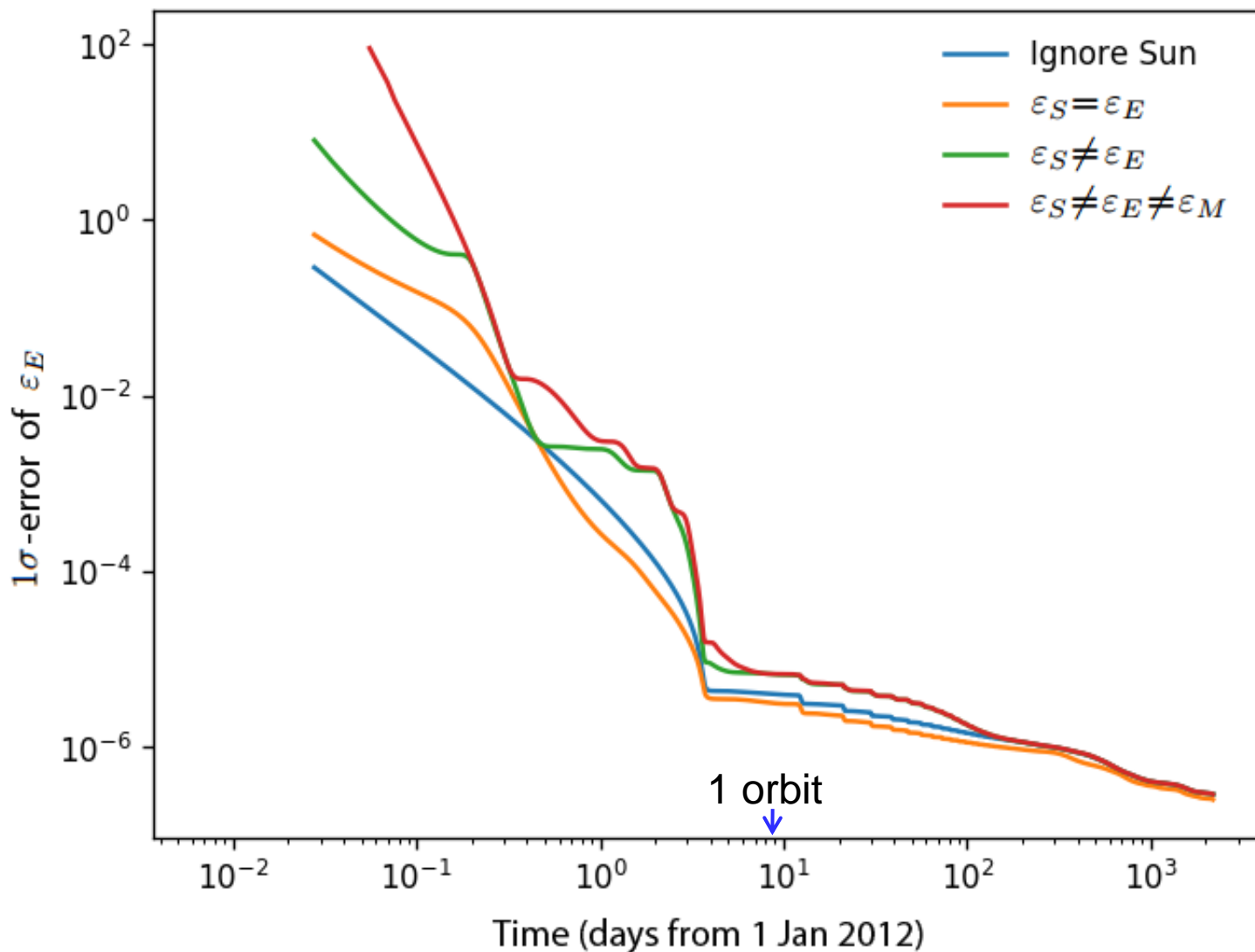
EEP violation due to other bodies is at first order in respective ΔU 's.

$$\frac{\Delta f_{\text{grav}}}{f} = \frac{\Delta U_E}{c^2} (1 + \varepsilon_E)$$

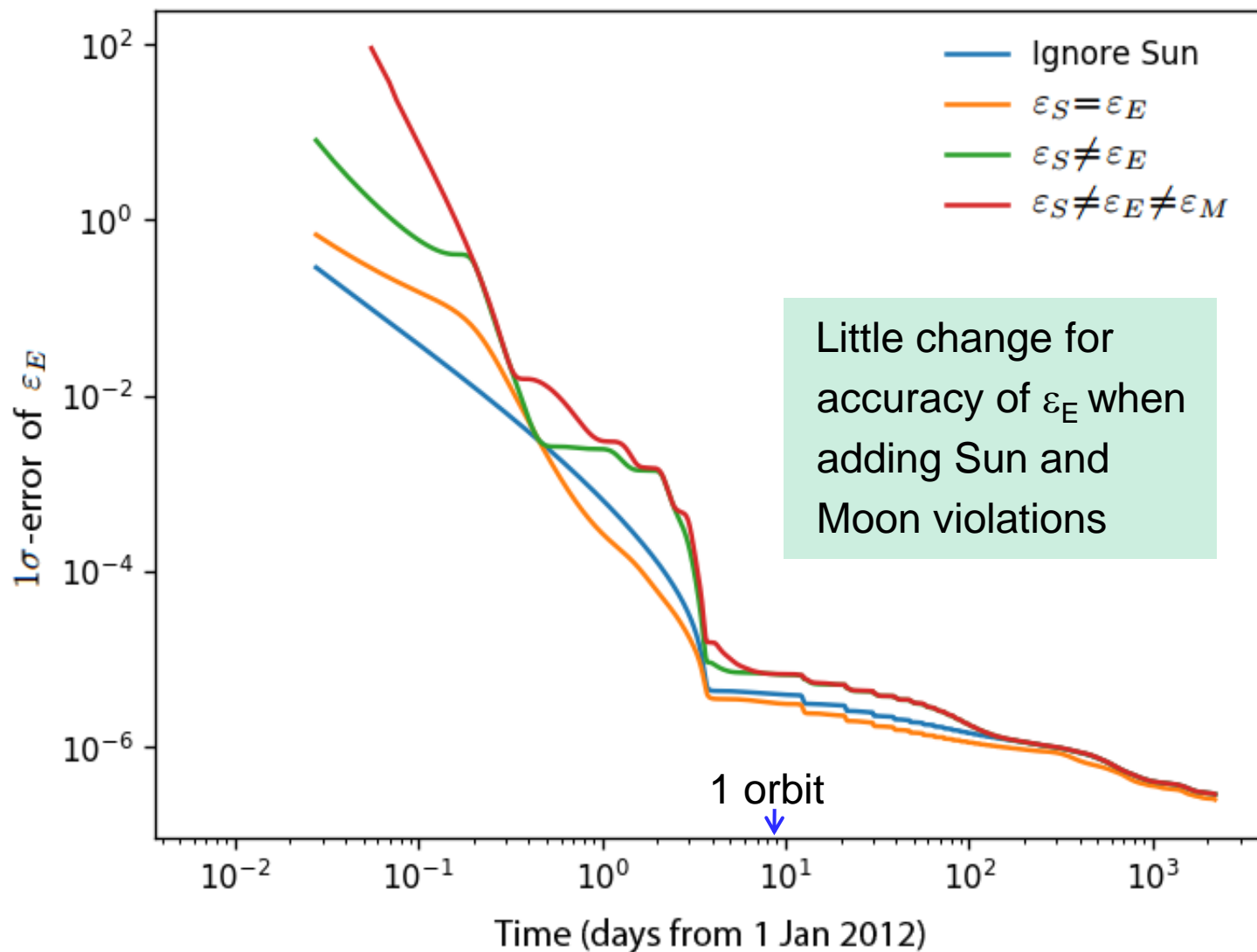


$$\frac{\Delta f_{\text{grav}}}{f} = \frac{\Delta U_E}{c^2} + \frac{\varepsilon_E \Delta U_E + \varepsilon_S \Delta U_S + \varepsilon_M \Delta U_M + \dots}{c^2}$$

E – Earth
S – Sun
M – Moon

Accuracy of measuring ε_E with RadioAstron – simulations

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Gravitational redshift experiments

Experiment	Launch/ Status	Frequency standard	Achieved/ expected $\delta\varepsilon$
Gravity Probe A	1976 completed	H-maser	1.4×10^{-4}
RadioAstron	2011 data processing	H-maser	$(1-2) \times 10^{-5}$
Galileo 5 & 6	2014 data processing	H-maser	$(3-4) \times 10^{-5}$
ACES	2020 to be launched	Cs-fountain + H-maser	$(2-3) \times 10^{-6}$

1. Observations finished: 62 measurements + 79 calibrations. Data analysis in progress.
2. Accuracy of 2×10^{-4} achieved in a single experiment (GP-A: 1.4×10^{-4})
3. Final accuracy of $\sim 10^{-5}$ seems realistic after full data analysis
4. One-way data analysis results: $\sim 10^{-3}$ as expected, systematics
5. Good news from the covariance analysis
6. Now taking into account the violation of Sun and Moon redshifts

Thank you!